

## Lecture 6 – Sensor Modeling

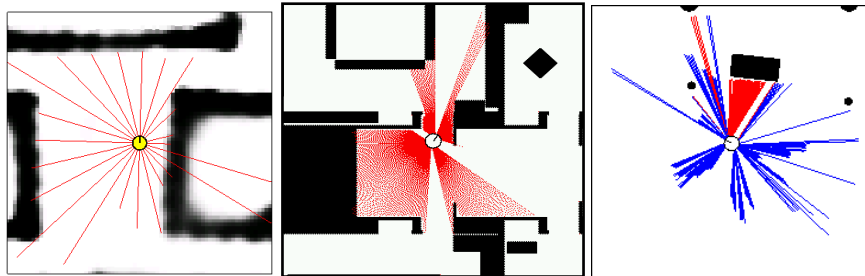
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### 1 – Probabilistic Sensor Models

- There are many sensors used in robotics
  - Contact sensors: Bumpers
  - Internal sensors
  - Accelerometers (spring-mounted masses)
  - Gyroscopes (spinning mass, laser light)
  - Compasses, inclinometers (earth magnetic field, gravity)
  - Proximity sensors
  - Sonar (time of flight)
  - Radar (phase and frequency)
  - Laser range-finders (triangulation, tof, phase)
  - Infrared (intensity)
  - Visual sensors: Cameras
  - Satellite-based sensors: GPS
- All have uncertainty
  - **Demo X80 !**
- How can we model this uncertainty?
- How can we determine  $p(z_t|x_t)$  that specifies the likelihood of a measurement  $z_t$  given a state  $x_t$  at time  $t$
- Or we can write  $p(z_t|x_t, m_t)$  where  $m_t$  is a map of the environment.
- Or, we can use the models  $z = Cx + \delta$ ,  $z = h(x) + \delta$

### 2 – Proximity Sensor Modeling

- Proximity sensors-that measure Range



- First note you may have  $K$  different measurements in one time step

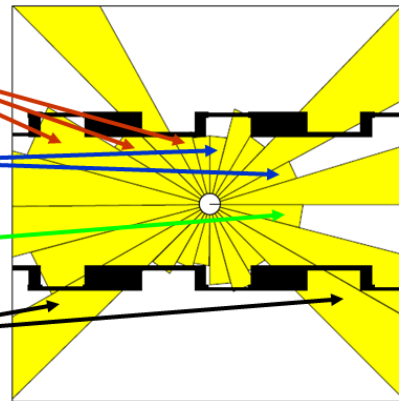
$$z = \{z_1, z_2, \dots, z_K\}$$

- We assume that each of these measurements are independent

$$P(z | x, m) = \prod_{k=1}^K P(z_k | x, m)$$

- Next, consider all the different sources of measurements
- Measurement can be caused by ...
  - a known obstacle.
  - cross-talk.
  - an unexpected obstacle (people, furniture, ...).
  - missing all obstacles (total reflection, glass, ...).

1. Beams reflected by obstacles
2. Beams reflected by persons / caused by crosstalk
3. Random measurements
4. Maximum range measurements

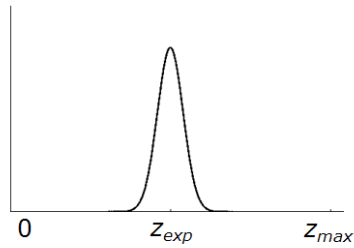


- Noise is due to uncertainty ...
  - in measuring distance to known obstacle.
  - in position of known obstacles.
  - in position of additional obstacles.
  - whether obstacle is missed.

### 3 – Constructing a Proximity Sensor model

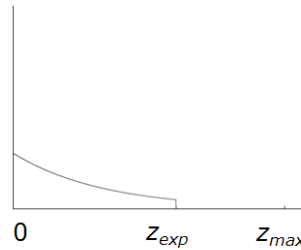
- Assume that with map we can get expected measurement  $z_{exp}$  or  $z^*$
- Model each source of measurement individually, then sum

Measurement noise



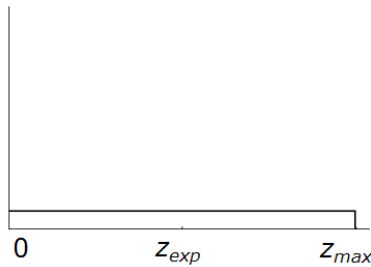
$$P_{hit}(z | x, m) = \eta \frac{1}{\sqrt{2\pi b}} e^{-\frac{1}{2} \frac{(z - z_{exp})^2}{b}}$$

Unexpected obstacles



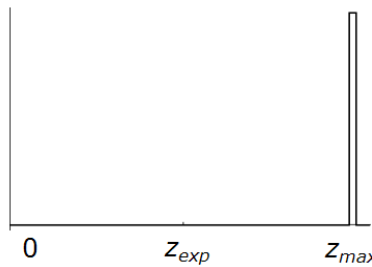
$$P_{unexp}(z | x, m) = \begin{cases} \eta \lambda e^{-\lambda z} & z < z_{exp} \\ 0 & \text{otherwise} \end{cases}$$

Random measurement



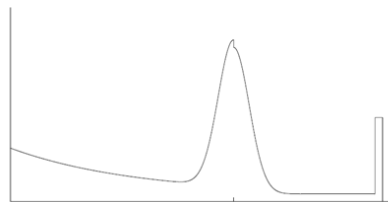
$$P_{rand}(z | x, m) = \eta \frac{1}{z_{max}}$$

Max range



$$P_{max}(z | x, m) = \eta \frac{1}{z_{small}}$$

- Resulting PDF



$$P(z | x, m) = \begin{pmatrix} \alpha_{hit} \\ \alpha_{unexp} \\ \alpha_{max} \\ \alpha_{rand} \end{pmatrix}^T \cdot \begin{pmatrix} P_{hit}(z | x, m) \\ P_{unexp}(z | x, m) \\ P_{max}(z | x, m) \\ P_{rand}(z | x, m) \end{pmatrix}$$

- How can we determine the alpha parameters?
  - $\alpha_{hit}$ ,  $\alpha_{unexp}$ ,  $\alpha_{max}$ ,  $\alpha_{rand}$ ,  $b$ , and  $\lambda$ .
- We can use maximum likelihood
  - System Identification techniques?
  - Least Squares?
  - Table 6.2 from text

#### 4 – Feature Based Measurement Models

- Consider the model  $z = h(x) + \delta$
- In this case  $z_t^i = [r_t^i \ \phi_t^i \ s_t^i]^T$ , where  $r$  is a range,  $\phi$  is a bearing and  $s$  is a signature of the  $i$ th feature
- Consider the  $j$ th map feature is defined by  $m^j = [mx^j \ my^j \ s^j]^T$
- Lets model this with respect to the robot pose  $[x \ y \ \theta]$

$$r_t^i = \text{sqrt}((mx^j - x)^2 + (my^j - y)^2) + \epsilon(\sigma_r^2)$$

$$\phi_t^i = \text{atan2}(my^j - y, mx^j - x) - \theta + \epsilon(\sigma_\phi^2)$$

$$s_t^i = s^j + \epsilon(\sigma_s^2)$$

- We can both calculate likelihood  $p(z|x,m)$

#### Algorithm landmark\_model\_known\_correspondence( $z_t^i, c_t^i, x_t, m$ )

$$j = c_t^i$$

$$r^{\text{exp}} = \text{sqrt}((mx^j - x)^2 + (my^j - y)^2)$$

$$\phi^{\text{exp}} = \text{atan2}(my^j - y, mx^j - x) - \theta$$

$$q = \text{prob}(r_t^i - r^{\text{exp}}, \sigma_r) * \text{prob}(\phi_t^i - \phi^{\text{exp}}, \sigma_\phi) * \text{prob}(s_t^i - s^j, \sigma_s)$$

return  $q$

- Note we could also do something like consider all bins.