Problem 1 Consider the following relations:

\[
R: \begin{array}{ccc}
A & B & C \\
\hline
b & c & 3 \\
c & c & 3 \\
c & a & 3 \\
b & b & 1 \\
c & a & 4 \\
b & a & 2 \\
\end{array}
\]

\[
S: \begin{array}{ccc}
A & B & C \\
\hline
c & c & 2 \\
c & a & 3 \\
b & b & 1 \\
a & b & 3 \\
b & c & 3 \\
a & a & 1 \\
c & c & 3 \\
\end{array}
\]

\[
T: \begin{array}{cccc}
B & D & E & F \\
\hline
a & a & 1 & 2 \\
c & d & 2 & 4 \\
b & b & 3 & 2 \\
d & b & 3 & 2 \\
a & a & 2 & 3 \\
b & c & 4 & 1 \\
d & a & 1 & 4 \\
\end{array}
\]

\[
W: \begin{array}{cc}
C & D \\
\hline
1 & a \\
2 & b \\
3 & c \\
4 & d \\
\end{array}
\]

For each of the following queries: (1) compute the answer, (2) draw the query tree.

a. \(R \cap S\)

b. \(S - R\)

c. \(R - S\)

d. \(\pi_{A,B}(S)\)

e. \(\pi_{B,C}(R) \cup \pi_{B,C}(S)\)

f. \(\pi_{A,B}(R) - \pi_{A,B}(S)\)

g. \(\pi_C(W) \times \pi_A(S) \times \pi_B(T)\)

h. \(\sigma_{E>F}(T)\)

i. \(\sigma_{A\neq B}(R)\)

j. \(\pi_{B,F}(\sigma_{F\geq E}(T))\)
k. \( \sigma_{A=D \lor B=D}(\pi_{A,B}(R) \times W) \)

l. \( \sigma_{A=b \land C>1}(R) \cup \sigma_{B=b \lor C\neq 3}(S) \)

m. \( \sigma_{-(B=d)}(T) \)

n. \( \pi_{A,B,R,C,D}(\sigma_{R,C=W}(R \times W)) \)

o. \( W \bowtie R \)

p. \( W \bowtie_{R,C=W} R \)

q. \( T \bowtie_{F>C} W \)

r. \( R \bowtie S \)

s. \( R \bowtie_{R,B=S,A} S \)

t. \( (R \bowtie T) \bowtie \pi_{A,C,D}(S \bowtie W) \)

u. \( \pi_{T1,D,T2,B}(\rho_{T1}(T) \bowtie_{T1,D=T2,B} \rho_{T2}(T)) \)

v. \( \pi_{B,D,E}(\sigma_{F\leq C}(T \bowtie W)) \)

w. \( \pi_{A,B}(R \bowtie_{R,C\neq S,C} S) \bowtie \sigma_{D=a}(T) \)

x. \( \pi_{A}(\pi_{B}(\pi_{C}(R \cup S))) \)

y. \( \sigma_{A\neq a}(S) \bowtie \sigma_{D\neq a}(W) \)

z. \( \sigma_{C=1}(R) \bowtie \sigma_{C=2}(S) \)
Problem 2  Consider the following database:

bands:

<table>
<thead>
<tr>
<th>Id</th>
<th>Name</th>
<th>Formed_in</th>
<th>Country</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>'Pink Floyd'</td>
<td>1965</td>
<td>'UK'</td>
</tr>
<tr>
<td>2</td>
<td>'King Crimson'</td>
<td>1969</td>
<td>'UK'</td>
</tr>
<tr>
<td>3</td>
<td>'Can'</td>
<td>1968</td>
<td>'Germany'</td>
</tr>
<tr>
<td>4</td>
<td>'Doors'</td>
<td>1967</td>
<td>'USA'</td>
</tr>
<tr>
<td>5</td>
<td>'Velvet Underground'</td>
<td>1967</td>
<td>'USA'</td>
</tr>
<tr>
<td>6</td>
<td>'Gong'</td>
<td>1969</td>
<td>'France'</td>
</tr>
<tr>
<td>7</td>
<td>'Yes'</td>
<td>1968</td>
<td>'UK'</td>
</tr>
</tbody>
</table>

albums:

<table>
<thead>
<tr>
<th>Aid</th>
<th>Title</th>
<th>BandId</th>
<th>Year</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>'Meddle'</td>
<td>1</td>
<td>1970</td>
</tr>
<tr>
<td>2</td>
<td>'Animals'</td>
<td>1</td>
<td>1977</td>
</tr>
<tr>
<td>3</td>
<td>'Red'</td>
<td>2</td>
<td>1974</td>
</tr>
<tr>
<td>4</td>
<td>'Landed'</td>
<td>3</td>
<td>1975</td>
</tr>
<tr>
<td>5</td>
<td>'Soundtracks'</td>
<td>3</td>
<td>1970</td>
</tr>
<tr>
<td>6</td>
<td>'Beat'</td>
<td>2</td>
<td>1982</td>
</tr>
<tr>
<td>7</td>
<td>'The Doors'</td>
<td>4</td>
<td>1967</td>
</tr>
<tr>
<td>8</td>
<td>'Strange Days'</td>
<td>4</td>
<td>1967</td>
</tr>
<tr>
<td>9</td>
<td>'Loaded'</td>
<td>5</td>
<td>1970</td>
</tr>
<tr>
<td>10</td>
<td>'You'</td>
<td>6</td>
<td>1974</td>
</tr>
<tr>
<td>11</td>
<td>'Shamal'</td>
<td>6</td>
<td>1976</td>
</tr>
<tr>
<td>12</td>
<td>'Fragile'</td>
<td>7</td>
<td>1971</td>
</tr>
<tr>
<td>13</td>
<td>'Close to the Edge'</td>
<td>7</td>
<td>1972</td>
</tr>
</tbody>
</table>

musicians:

<table>
<thead>
<tr>
<th>MId</th>
<th>Name</th>
<th>BandId</th>
<th>From</th>
<th>To</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>'Roger Waters'</td>
<td>1</td>
<td>1966</td>
<td>1983</td>
</tr>
<tr>
<td>2</td>
<td>'Syd Barrett'</td>
<td>1</td>
<td>1966</td>
<td>1968</td>
</tr>
<tr>
<td>3</td>
<td>'Robert Fripp'</td>
<td>2</td>
<td>1969</td>
<td>2002</td>
</tr>
<tr>
<td>4</td>
<td>'Adrian Belew'</td>
<td>2</td>
<td>1981</td>
<td>2002</td>
</tr>
<tr>
<td>5</td>
<td>'Irmin Schmidt'</td>
<td>3</td>
<td>1968</td>
<td>1978</td>
</tr>
<tr>
<td>6</td>
<td>'Michael Karoli'</td>
<td>3</td>
<td>1968</td>
<td>1978</td>
</tr>
<tr>
<td>7</td>
<td>'Jim Morrison'</td>
<td>4</td>
<td>1967</td>
<td>1971</td>
</tr>
<tr>
<td>8</td>
<td>'Lou Reed'</td>
<td>5</td>
<td>1967</td>
<td>1973</td>
</tr>
<tr>
<td>9</td>
<td>'Daevid Allen'</td>
<td>6</td>
<td>1969</td>
<td>1974</td>
</tr>
<tr>
<td>10</td>
<td>'Pierre Moerlen'</td>
<td>6</td>
<td>1975</td>
<td>1978</td>
</tr>
<tr>
<td>11</td>
<td>'Jon Anderson'</td>
<td>7</td>
<td>1968</td>
<td>1981</td>
</tr>
<tr>
<td>12</td>
<td>'Bill Bruford'</td>
<td>7</td>
<td>1968</td>
<td>1972</td>
</tr>
<tr>
<td>13</td>
<td>'Bill Bruford'</td>
<td>2</td>
<td>1972</td>
<td>2010</td>
</tr>
</tbody>
</table>

Notes:  (a) BandId is a foreign key on bands in both relations where this attribute appears.  
(b) Consider all attributes indicating years to be integers with appropriate comparison operators applicable.  
(c) In what follows we assume that if a musician is listed as being in the band during a year in which an album was recorded, the musician played on it.  
(d) First attribute of each relation is its primary key.
If you need to refer to relation names in queries you can use A for albums, B for bands and M for musicians.

Translate the following queries into Relational Algebra and compute their answers based on the given database. As an extra exercise, draw the query trees for the relational algebra expressions you construct.

1. Find all musicians who played with their band in year 1970. Output the names of the musicians.
2. Find all musicians who played with their band in year 1970. Output the names of the musicians and the name of the band they played in.
3. Find all musicians who played for 'Gong'. Output the names of the musicians and the years they played in the band.
4. Find all musicians who played in the band 'King Crimson' in the year 1974. Output the names of the musicians.
5. Find all musicians who played in their band in the band's year of inception. Output the names of the musicians and the names of the bands.
6. Find the band that released the album 'Loaded'. Report the name of the band.
7. Find the band in which 'Jim Morrison' played. Report the name of the band.
8. Find all albums recorded by bands from UK. For each record output its name, year and the name of the band that recorded it.
9. Find all musicians who participated in recording of the album 'Fragile'. Output the names of the musicians.
10. Find all 'Pink Floyd' band members who did NOT participate in the recording of the album 'Meddle'. (note: a musician did not participate in a recording of an album if he did not play in the band that year).
11. Find all bands that recorded two albums in the same year. For each band, output its name, titles of both albums and the year of their release.
12. Find all bands in which 'Lou Reed' DID NOT play. Output the names of the bands.
13. Find all albums recorded by the bands that had at least one musician leave before 1972. Output the name of the album and the year of release.
14. Find all albums recorded by 'King Crimson' before 'Adrian Belew' joined the band. Report the album titles and years.
15. Find all musicians who played in at least two different bands. Report their names.