# **Problem-Solving Agents**

#### Subclass of goal-based agents

#### goal formulation

#### problem formulation

#### example problems

- toy problems
- real-world problems

#### search

- search strategies
- constraint satisfaction

#### solution

# **Goal Formulation**

#### Specify the objectives to be achieved

#### goal

a set of desirable world states in which the objectives have been achieved

#### current / initial situation

starting point for the goal formulation

#### actions

cause transitions between world states

## **Problem Formulation**

#### Actions and states to consider

states possible world states

accessibility the agent can determine via its sensors in which state it is

consequences of actions the agent knows the results of its actions

**levels** problems and actions can be specified at various levels

**constraints** conditions that influence the problem-solving process

performance measures to be applied

costs utilization of resources

Example: vacuum world, restricted to two locations with two states (dirty, clean)

# **Problem Types**

#### Not all problems are created equal

single-state problem

multiple-state problem

contingency problem

exploration problem

# Single-State Problem

#### exact prediction is possible

#### state

is known exactly after any sequence of actions

accessibility of the world
 all essential information can be obtained
 through sensors

**consequences** of actions are known to the agent

#### goal

for each known initial state, there is a unique goal state that is guaranteed to be reachable via an action sequence

simplest case, but severely restricted

Example: Vacuum world, [?]p. 58
Limitations: Can't deal with
incomplete accessibility
incomplete knowledge about consequences
changes in the world
indeterminism in the world, in actions

## Multiple-State Problem

#### semi-exact prediction is possible

**state** is *not* known exactly, but limited to a set of possible states after each action

accessibility of the world
 not all essential information can be obtained
 through sensors
 reasoning can be used to determine the set of
 possible states

consequences of actions

are not always or completely known to the agent; actions or the environment might exhibit randomness

**goal** due to ignorance, there may be no fixed action sequence that leads to the goal

less restricted, but more complex

Example: Vacuum world, [?]p. 58, but the agent has *no* sensors

The action sequence right, suck, left, suck is guaranteed to reach the goal state from any initial state

Limitations: Can't deal with changes in the world during execution ("contingencies")

### **Contingency Problem**

#### exact prediction is impossible

**state** unknown in advance, may depend on the outcome of actions and changes in the environment

accessibility of the world some essential information may be obtained through sensors only at execution time

**consequences** of actions may not be known at planning time

**goal** instead of single action sequences, there are *trees of actions* 

contingency branching point in the tree of actions

**agent design** different from the previous two cases: the agent must act on incomplete plans

search and execution phases are interleaved

Example: Vacuum world, [?]p. 58, The effect of a suck action is random. There is no action sequence that can be calculated at planning time and is guaranteed to reach the goal state.

Limitations: Can't deal with

situations in which the environment or effects of action are unknown

## **Exploration Problem**

#### effects of actions are unknown

#### state

the set of possible states may be unknown

#### accessibility of the world

some essential information may be obtained through sensors only at execution time

#### consequences of actions

may not be known at planning time

# **goal** can't be completely formulated in advance because states and consequences may not be known at planning time

#### discovery

what states exist

#### experimentation

what are the outcomes of actions

#### learning

remember and evaluate experiments

#### agent design

different from the previous cases: the agent must experiment

#### search

requires search in the real world, not in an abstract model

realistic problems, very hard

### **Well-Defined Problems**

#### exact formulation of problems and solutions

#### initial state

current state / set of states, or the state at the beginning of the problem-solving process must be known to the agent

#### operator

description of an action

#### state space

set of all states reachable from the initial state by a possible sequence of actions

#### path in the search space

sequence of actions between two states

#### goal test

determines if the agent has reached a goal state

#### path cost

function that assigns a cost to a path usually the sum of the costs of actions along

#### the path

#### data type PROBLEM

**components:** Initial-State, Operators, Goal-Test, Path-Cost

#### solution

path from the initial state to a state that satisfies the goal test

#### search algorithm

takes the problem data type and computes a solution

basis for a formal treatment

# Performance Measuring

#### for problem solving

#### success

Has a solution been found?

#### quality

Is it a good solution? What are the criteria?

#### optimal solution

may be difficult to find and not necessary

#### cost

sum of

- search cost (time, resources to find a solution)
- path cost (as defined above)

# toy problems

vacuum world	
8-queens	
8-puzzle	
missionaries and cannibals	

Franz J. Kurfess, CAL POLY SLO

# Vacuum World

#### simplified version

two squares, either dirty or clean, vacuum has sensors

#### states

location of vacuum, squares dirty or clean

#### operators

move left, move right, suck

#### goal test

all squares clean

#### path cost

1 unit per action

see Figure 3.2, 3.6 in [?], p. 66

# 8-Queens

#### no queen attacks any other

#### states

arrangement of 8 queens on the board

#### operators

add a queen

#### goal test

no queen attacked

#### path cost

zero (irrelevant, all solutions are equally good)

restrictions on the states and operators can lead to vastly different search spaces

incremental version; complete-state formulation moves queens around [?]page 64

### Real-World Problems

#### route finding

travel advisory, computer networks, airline travel

#### travelling salesperson

each city must be visited exactly once more complex than route finding

#### **VLSI** layout

positioning of gates and connections too complex for humans crucial for successfull operation and costs

#### robot navigation

generalization of route finding to continuous space, possibly multi-dimensional (actions involving arms)



#### Examine possible sequences of actions

#### input

problem description, initial state

#### output

solution as an action sequence

#### search space

set of all possible action sequences



#### in Artificial Intelligence

#### search of a problem space

for a solution to a problem *not:* search through data structures

#### basic idea:

find a path from the initial description of a problem to a description of the solved problem

problem space is created incrementally,
 not predefined and already in existence

#### problem-solving method

powerful technique for many different areas

# **Problem Space**

#### Representation

#### Network

graph with nodes as states and arcs as possible steps
unique representations of states, multiple
incoming arcs

#### Tree

multiple representations of states



#### different ways to search

#### random search

next step is selected randomly from the possible ones non-systematic; can't guarantee complete coverage of the search space; paths may be selected multiple times; may take infinite time

#### blind search

systematic approach; no knowledge about closeness to the solution; complete coverage; ineffective if closeness to solutions can be measured

#### directed search

systematic approach; paths leading towards the solution are preferred

### **Search Methods**

#### used in AI problems

#### depth-first

blind, systematic expands each path to the end, backtracking when a dead end is encountered

#### breadth-first

blind, systematic all nodes at one level are expanded finds the shortest path

#### beam search

directed, heuristic variation of breadth-first only a limited number of nodes are expanded all successor nodes are evaluated, the best ones are selected for expansion

#### hill-climbing

directed variation of depth-first successor node with the greatest progress towards the goal is selected problems: local maxima, plateaus, ridges

#### branch and bound

directed search
most promising node in the tree is selected
finds the shortest path
problem: significant portion of the search tree
must be expanded

#### best-first

directed, heuristic search algorithm requires estimate of the distance to the solution selects the node with the smallest estimate *problem:* does not take into account the length of already expanded parts of the paths

#### **A**★ (A-Star)

combination of best-first and branch and bound requires estimate of the distance to the solution uses estimate and previous path length to calculate the cost if estimates are always greater than zero but never greater than the actual cost, the lowest cost path will be found reduces the number of nodes expanded by best-first



#### Action sequence that satisfies the goal

#### validation

Does the solution really achieve the goal?

#### verification

Is the sequence of actions admissible?

#### feasibility

With the available resources, can the sequence of actions be carried out?

#### execution

actions are carried out

# Summary

#### Problem-Solving Agents

#### goal formulation

objectives that need to be achieved

#### problem formulation

actions and states to consider

#### problem types

single-/multiple state, contingency, exploration

**example problems** toy problems real-world problems

**search** strategies

#### solution

execution of the action sequence